

A Protein Substructure Based P System for Description and Analysis of Cell Signalling Networks

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7th Workshop on
Membrane Computing



Outline

Bringing Membrane Systems Back to Biology

Introduction

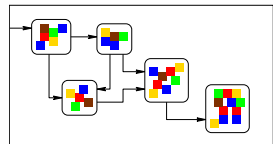
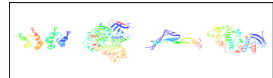
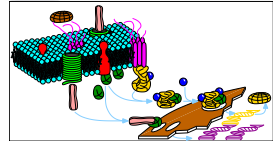
Biological Principles of Cell Signalling
ESIGNET – Research Project
Modelling Cell Signalling Networks

A P System for Cell Signalling Networks

Motivation and Intention
System Definition
Matching and Matching Strategies
System Behaviour and Properties

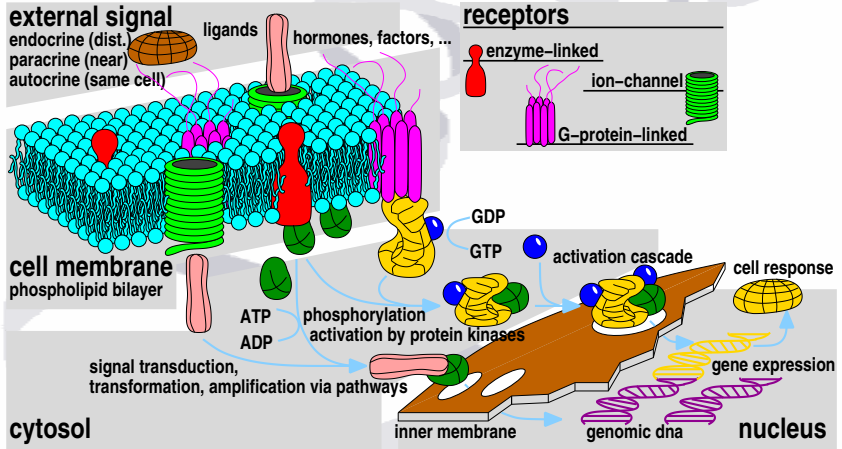
Example and Conclusion

Example: Yeast Pheromone Pathway
Conclusion and Future Work



Biological Principles of Cell Signalling

Information Processing in Living Cells



ESIGNET – Research Project

Evolving Cell Signalling Networks (CSNs) *in silico*

European interdisciplinary research project

- University of Birmingham (Computer Science)
- TU Eindhoven (Biomedical Engineering)
- Dublin City University (ALife Lab)
- University of Jena (Bio Systems Analysis)



SIXTH FRAMEWORK
PROGRAMME



TU/e

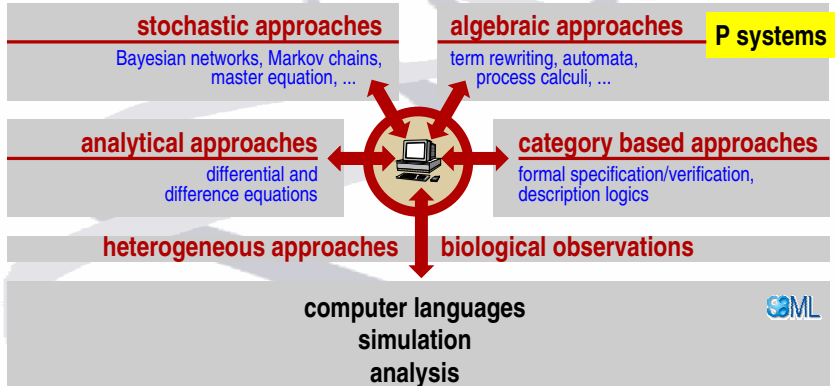
Objectives

- study the computational properties of CSNs
- developing new ways to model and predict real CSNs
- gain new theoretical perspectives on real CSNs



Modelling Cell Signalling Networks

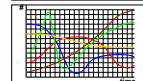
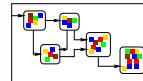
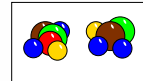
Phenotypic Description of CSNs – Structure, Behaviour, Function



Motivation and Intention

Adopting Advantages of P Systems to Project Objectives

- Capture significant aspects of cellular signalling:
 - components, topology, modularity
 - protein substructures and properties
 - dynamical behaviour
 - signal coding and transduction
 - robustness to perturbations
 - computational capacity
- Provide a general framework
- P systems feature different levels of abstraction
- Keep formalism tractable
- Balance detailedness with computational needs
- Facilitate system modification, recombination, and construction ab initio



1	0	0	1	1	0	0
0	1	1	0	0	1	0
1	0	1	1	0	1	0
1	0	0	1	0	0	1

System Definition

Identification of Components Based on Biological Model

- System $\Pi_{\text{CSN}} = (V, V', E, M, n)$
 - V : alphabet of protein identifiers
 - V' : alphabet of protein substructure/property identifiers
 - M : **modules** \longrightarrow functional reaction units
 - E : graph \longrightarrow transduction **channels** between modules
 - n : number of modules (degree of the P system)
- Modules $M_i = (R_{i1}, \dots, R_{ir_i}, f_{i1}, \dots, f_{ir_i}, A_i) \in M$
 - R_{ij} : reaction rule \longrightarrow multisets of educts and products may contain meta-symbols \longrightarrow **matching** required
 - f_{ij} : function corresponding to **kinetics** of R_{ij} , number of educt objects taken from module within one reaction step
 - A_i : multiset of axioms \longrightarrow initial contents of M_i
- Channels $e_{ij} = (i, j, l_{ij}, d_{ij}) \in E$
 - weighted directed channel from module i to module j
 - l_{ij} : filter interface (**receptor pattern** and **conc. gradient**)
 - d_{ij} : time **delay** (number of system **steps**) for passage

Matching and Matching Strategies

Comparison of String-Objects Describing Biomolecules

- String-based representation of proteins
 - string-object** s : representation of a protein, its properties, substructure, binding domains, activation state, ligands
 - structure**: $s \in V^+ \otimes (\{\#\} \otimes ((V')^+ \cup \{\neg\} \otimes (V')^+ \cup \{*\}))^*$
 - meta-symbols**: **placeholder** (wild-card) $*$ \rightarrow appropriate or unknown substructure/property; **exclusion** \neg
 - test whether two string-objects identify same molecule
- Matching strategies

loose:

two string-objects match iff there is at least one common wild-card free representation

							concretions					
C α #GDP#p	C α #GDP#-p	C α #GTP#p	C α #GTP#-p	C α #*#p	C α #GDP#*	C α #*#*	D β E#*#*					
■								C α #GDP#p	■			
■	■							C α #GDP#-p		■		
		■						C α #GTP#p			■	
			■					C α #GTP#-p				■
■	■	■	■	■	■	■	■	C α #*#p	■	■	■	■
■	■	■	■	■	■	■	■	C α #GDP#*	■	■	■	■
■	■	■	■	■	■	■	■	C α #*#*	■	■	■	■
						■	■	D β E#*#*				■

$V = \{C\alpha, D\beta E\}$
 $V' = \{GDP, GTP, p\}$

Loose matching
strict matching

strict:

participating string-objects interpreted as a pattern and a candidate (concretion of the pattern)



Matching and Matching Strategies

Comparison of String-Objects Describing Biomolecules

								concretions							
$C\alpha\#GDP\#p$	$C\alpha\#GDP\#\neg p$	$C\alpha\#GTP\#p$	$C\alpha\#GTP\#\neg p$	$C\alpha\#\#\#p$	$C\alpha\#GDP\#\#$	$C\alpha\#\#\#\#$	$D\beta:E\#\#\#$	$C\alpha\#GDP\#p$	$C\alpha\#GDP\#\neg p$	$C\alpha\#GTP\#p$	$C\alpha\#GTP\#\neg p$	$C\alpha\#\#\#p$	$C\alpha\#GDP\#\#$	$C\alpha\#\#\#\#$	$D\beta:E\#\#\#$
■				■	■	■		■							
	■				■	■			■						
		■		■		■				■					
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■	■	■	■	■	■	■		■	■	■	■	■	■	■	
							■								■

$V = \{C\alpha, D\beta:E\}$
 $V' = \{GDP, GTP, p\}$

patterns

loose matching

strict matching

System Behaviour and Properties

Controlled Interplay of Components at Global Level

- Definition of dynamical system behaviour
 - contents of module M_i at global time $t \in \mathbf{N}$: multiset $L_i(t)$
 - system step by module M_i :

$$L_i(0) = A_i$$

$$L'_i(t) = L_i(t) \ominus \text{Educts}_i(t) \uplus \text{Products}_i(t)$$

$$L_i(t+1) = L'_i(t) \ominus \text{Outgoing}_i(t) \uplus \text{Incoming}_i(t)$$

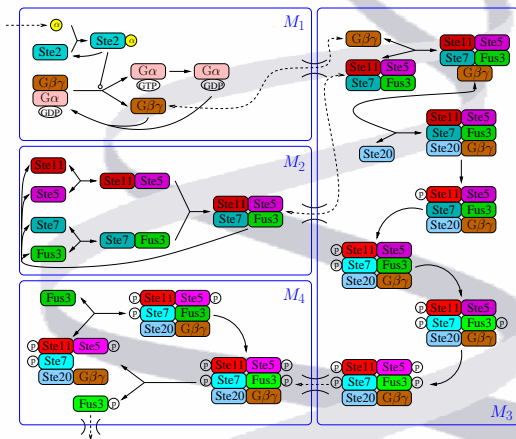
1. Determine multiset of educts using $L_i(t), R_{i1}, \dots, R_{ir_i}, f_{i1}, \dots, f_{ir_i}$; involves matching
2. Remove educt objects from module contents
3. Determine and add multiset of reaction products, obtain $L'_i(t)$
4. Determine and separate objects leaving host module evaluate $L'_i(t)$ and I for each outgoing channel, matching
5. Add objects received from incoming channels, consider d

- System properties
 - modularity – static system topology – ability to identify objects/substructures – flexibility in level of abstraction
 - determinism – computational tractability – universality

Example: Yeast Pheromone Pathway

Signal Transduction in *Saccharomyces cerevisiae*

A well-known signalling system controlling mating behaviour

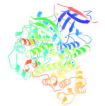


$$\begin{aligned} \Pi &= (V, V', E, M, 4) \\ V &= \{\text{Ste2}, \alpha, \text{G}\beta\gamma, \text{G}\alpha, \dots\} \\ V' &= \{a, \text{GDP}, \text{GTP}, p\} \\ M &= \{M_1, M_2, M_3, M_4\} \\ M_1 &= (R_{11}, R_{12}, R_{13}, R_{14}, R_{15}, \\ &\quad f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, A_1) \\ R_{11} &= \text{Ste2}\# \neg a + \alpha \rightarrow \text{Ste2}\# a \\ R_{12} &= \text{Ste2}\# a \rightarrow \text{Ste2}\# \neg a \\ f_{11} &= [k_{11}[\text{Ste2}\# \neg a][\alpha]/V_1^2] \\ &\vdots \end{aligned}$$

Conclusion and Future Work

Summary

- P systems provide a suitable framework for modelling CSNs
- Valuable insight can be gained from combining previously isolated ideas
- Our system takes first steps in this direction



Outlook

- Software simulation to prove practicability of the approach
- Interface to biological databases / experimental knowledge
- Investigation into the evolution of CSNs

